

Modelling Normal Tissue Isoeffect Distribution in Conformal Radiotherapy of Glioblastoma Provides an Alternative Dose Escalation Pattern through Hypofractionation without Reducing the Total Dose

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The purpose of this study was to prove that by using conformal external beam radiotherapy (RT) normal brain structures can be protected even when applying an alternative approach of biological dose escalation: hypofractionation (HOF) without total dose reduction (TDR). Traditional 2-dimensional (2D) and conformal 3-dimensional (3D) treatment plans were prepared for 10 gliomas representing the subanatomical sites of the supratentorial brain. Isoeffect distributions were generated by the biologically effective dose (BED) formula to analyse the effect of conventionally fractionated (CF) and HOF schedules on both the spatial biological dose distribution and biological dose-volume histograms. A comparison was made between 2D-CF (2.0 Gy/day) and 3D-HOF (2.5 Gy/day) regimens, applying the same 60 Gy total doses. Integral biologically effective dose (IBED) and volumes received biologically equivalent to a dose of 54 Gy or more (V-BED₅₄) were calculated for the lower and upper brain stem as organs at risk. The IBED values were lower with the 3D-HOF than with the 2D-CF schedule in each tumour location, means 22.7 ± 17.1 and 40.4 ± 16.9 in Gy, respectively ($p < 0.0001$). The V-BED₅₄ values were also smaller or equal in 90% of the cases favouring the 3D-HOF scheme. The means were 2.7 ± 4.8 cc for 3D-HOF and 10.7 ± 12.7 cc for 2D-CF ($p = 0.0006$). Our results suggest that with conformal RT, fraction size can gradually be increased. HOF radiotherapy regimens without TDR shorten the treatment time and seem to be an alternative way of dose escalation in the treatment of glioblastoma.

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External beam radiotherapy (RT) is considered to be the routine treatment for malignant gliomas, but the results with this method are disappointing (1, 2). Efforts have been made to escalate dose in order to improve local control (3, 4). Image-based 3-dimensional (3D) conformal RT ensures a significant reduction in treated volume in order to spare the surrounding normal tissues (5, 6). Patients with brain tumours are ideal candidates for 3D focal RT, because the skull can be immobilized and non-coplanar beams can be used (7, 8). Moreover, using the shrinking field technique, the dose gradient can be further increased between neoplastic-potentially infiltrated and normal tissues (9). Since focal RT techniques can allow a higher optimum dose per fraction while preserving a given normal tissue isoeffect (10–12), our assumption was that by using 3D conformal techniques, an acceptable protection of the organs at risk can be achieved even in a hypofractionated (HOF) regimen, with a gradual increase of single doses and without the

necessity of reducing the total dose. Therefore this technique and the fractionation schedule were compared with traditional 2-dimensional (2D) treatment planning based conventionally fractionated (CF) RT of a 60 Gy total dose.

Radiobiological modelling can be suitable for estimating the effect of altered fractionation schedules on normal tissue complication probabilities and an isoeffect distribution model can be applicable for judging the spatial effect of different fractionation regimens (13–16). As representative organs at risk, the midline structures are considered to be more sensitive to radiation than other parts of the normal brain (5, 17, 18). In the majority of cases, focal radionecrosis in the supratentorial lobar brain can be treated by salvage neurosurgery, but those in the midline structures cannot be treated in this way (1, 19). Therefore, in this study we examined the biologically effective dose to the midline structures with CF and HOF radiotherapy regimens.

MATERIAL AND METHODS

Target volumes and critical structures

CT images of 10 glioma patients were used for the investigation. The locations of the tumours represent the sub-anatomical sites of the supratentorial brain (Fig. 1). Five of the tumours originated in the parafalcine regions (parafalcine location) from the frontal to the occipital poles. The other five tumours at least partially infiltrated the temporal lobe (temporal location), whose location generally possesses difficulty in the traditional RT planning (1). The primary planning target volume (PTV₁) was defined as gross tumour volume (i.e. contrast-enhancing area) with a margin of 2.5–3 cm, while the boost planning target volume (PTV₂) was outlined with a 1.0–1.5 cm margin. The mean volume of PTV₁-s was 371.7 cm (range: 218.6–505.0 cm), and the mean volume of the PTV₂-s was 69.4 cm (range: 32.4–195.2 cm). Target volumes are listed in detail in the caption to Fig. 1. The lower and the upper brain stems were defined as critical structures. The lower brain stem (LBS) included the mid-brain, the pons and the medulla oblongata, ending at the level of the first cervical segment of the spinal cord (± 5 mm). The upper brain stem (UBS) included parts of

diencephalon: structures surrounding the third ventricle, the thalamus, the hypothalamus and the basal ganglia. The mean volumes of the LBS and UBS were 36.9 cm (range: 33.5–40.8 cm) and 30.2 cm (range: 26.0–37.7 cm), respectively. PTV₁ partially involved some parts of the UBS in each case and of the LBS in 4 cases (patients 4, 5, 6 and 8; see Fig. 1). The PTV₂ involved a part of UBS in 2 cases (patients 6 and 8; see Fig. 1).

Treatment planning

The dose calculation was based on 3D options by the Voxelpian treatment planning system. Both traditional 2D and conformal 3D treatment plans were generated for each target volume, taking care of organs at risk as far as possible. In the 2D plans non-conformal coplanar fields were used, taking into consideration the largest diameters of target volumes. Frequently, we selected the opposed weighted field technique to avoid radiation injury to the eyes. The 3D plans included three or four conformal non-coplanar fields; 6 MV or 18 MV photon energies were selected, depending on the location of the target volume. The 2 Gy reference dose was prescribed to 90% of the maximum dose. The mean relative doses in the PTV₁-s were 94.1% (range: 92.6–96.0%) and 94.0% (range: 91.9–

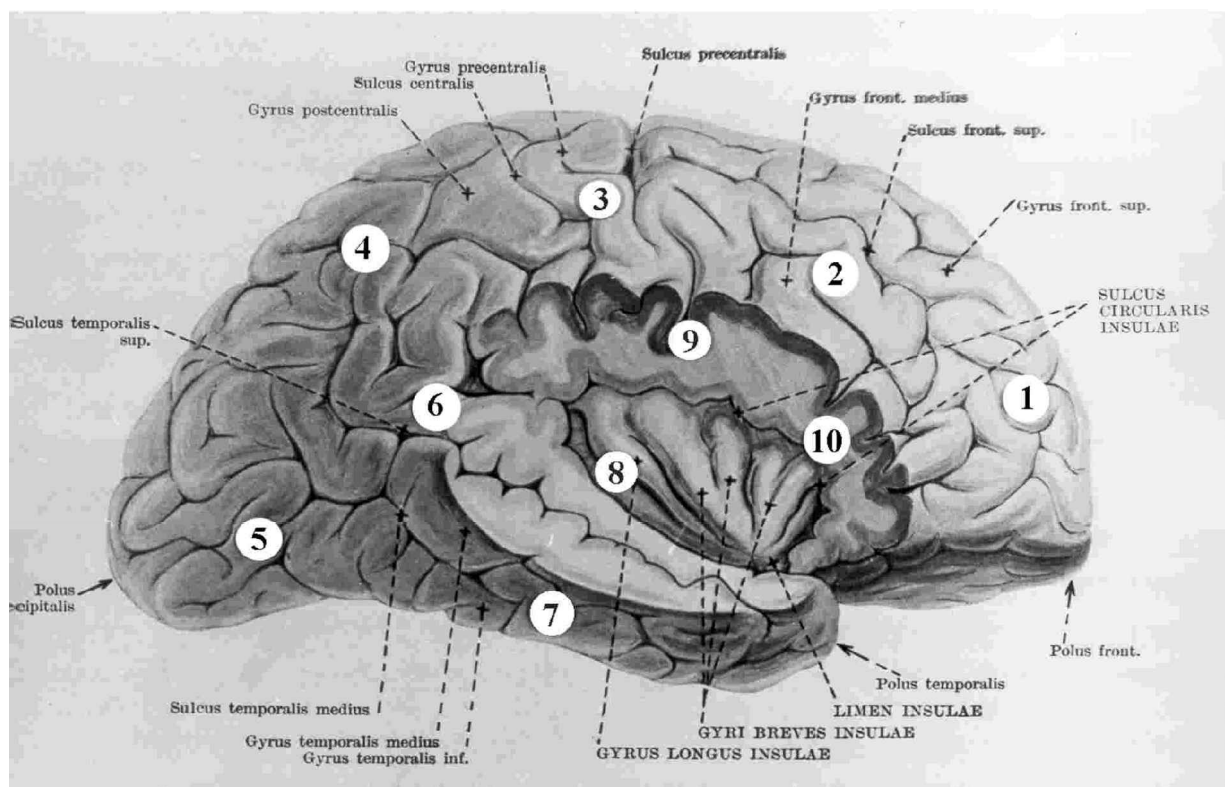


Fig. 1. Anatomical location of suprasellar brain tumours in 10 patients: frontobasal (1); fronto-parietal (2); parietal-parafalcine (3); parieto-occipital (4); occipital (5); temporo-parieto-occipital (6); temporal (7); deep temporal-insular (8); temporo-parietal (9); fronto-temporo-parietal (10). Primary and boost target volumes in cm: (1) 397.3 and 46.0; (2) 505.0 and 50.6; (3) 319.3 and 47.2; (4) 476.7 and 65.4; (5) 422.7 and 79.1; (6) 390.0 and 195.2; (7) 419.1 and 32.4; (8) 298.6 and 45.1; (9) 218.6 and 48.2; (10) 269.5 and 85.0 + 69.5 (bifocal tumour), respectively.

96.6%) in the 2D and 3D plans, respectively, while in the PTV₂-s the respective values were 94.4% (range: 91.8–97.5%) and 94.5% (range: 92.3–95.6%). Simulating the shrinking field technique, the absolute dose values from extended and boost fields were supplemented with 0.75/0.25 weightings in each case.

Biological modelling

The calculated data of physical dose distribution were transformed to biological dose data applying a radio-biological equivalence equation. Thus, biologically adapted dose-volume histograms (DVHs) and 3D biological dose distribution were generated; 2.0 Gy was chosen for the α/β ratio of late effects of the normal brain tissues (20). As suggested by others, the biologically effective dose (BED) formula based on the linear quadratic (LQ) model was utilized: $BED = D(1 + d/(\alpha/\beta))$, where D and d are the total dose and fraction size, respectively (15, 20, 21). Applying this equation to the conventional fractionation schemes results in the LQED₂ formula (linear quadratic equivalent dose for 2 Gy fractions) and this was used in our investigation: $LQED_2 = D(\alpha/\beta + d)/(\alpha/\beta + 2)$ where D and d are the same as before (21).

The traditional 2D treatment plans with daily 2.0 Gy fraction size (2D-CF) and the 3D conformal plans with daily 2.5 Gy fraction size (3D-HOF) using the same total dose of 60 Gy (45 Gy + 15 Gy boost dose) were compared. To simulate the daily practice in the shrinking field technique, the biologically transformed data were added in the proportion 0.75/0.25, as partial biologically effective doses (22). In the 3D-HOF method, in addition to the successive regimen, the simultaneous approach was also tested in order to decrease the biological effect of HOF in organs at

risk. Finally, the concomitant boost irradiation form was chosen for the detailed comparison, when the physical doses were added first, and the biological transformation was performed afterwards.

Calculation of dose to midline structures

The biological doses to the lower and upper brain stem with 2D-CF and 3D-HOF regimens were compared. First, the integral biologically effective dose (IBED) to midline structures was determined using the formula devised by Clark et al.: $IBED = \sum d_i(1 + d_i/(\alpha/\beta))\Delta v_i/V$, where i is 1% dose band, d_i is the ith dose band, Δv_i is the volume within each dose band and V is the total dose of the structure (23).

A biological equivalent dose of 54 Gy was selected as a tolerable dose to the normal brain, based on previous reports (5, 17). Volumes of the midline structures which received a biologically equivalent dose equal to or greater than 54 Gy (V-BED54) were calculated. Biologically transformed DVHs were generated to calculate the V-BED54. The percentage of the V-BED54 to the whole midline structures as 'high-dose regions' was also determined.

RESULTS

The IBED values of the LBS and UBS for the two treatment methods are listed in Table 1. The IBED values were lower with the 3D-HOF than with the 2D-CF schedule in each tumour location, means 22.7 ± 17.1 and 40.4 ± 16.9 in Gy, respectively ($p < 0.0001$). The V-BED54 values of the midline structures are presented in Table 2. These volumes with the 3D-HOF regimen are equal to, or lower than those with the 2D-CF regimen in 90% of cases (18 out of 20). The means were 2.7 ± 4.8 ccm for 3D-HOF and

Table 1

Integral biologically effective dose to the midline structures in Gy with 2D-CF (daily 2.0 Gy fraction size) and with 3D-HOF (daily 2.5 Gy fraction size) treatments by anatomical location of tumour

	Lower brain stem		Upper brain stem	
Location of tumour	2D-CF	3D-HOF	2D-CF	3D-HOF
1. Frontobasal	18.3	7.5	50.7	48.2
2. Fronto-parietal	17.5	3.8	50.5	14.3
3. Parietal-parafalcial	4.4	1.7	48.2	23.9
4. Parieto-occipital	16.3	6.1	48.6	33.3
5. Occipital	31.6	5.1	35.3	10.5
Average of 1–5.	17.6 ± 9.6	4.8 ± 2.2	46.7 ± 6.4	26.0 ± 15.2
6. Temporo-parieto-occipital	43.5	23.2	59.8	50.2
7. Temporal	45.8	18.1	58.5	39.3
8. Deep temporal	38.9	15.8	59.3	53.9
9. Temporo-parietal	33.4	9.6	59.3	39.4
10. Fronto-temporo-parietal	27.4	10.7	60.4	40.1
Average of 6–10	37.8 ± 7.5	15.5 ± 5.6	59.5 ± 0.7	44.6 ± 7.0
Average of 1–10	27.7 ± 13.4	10.2 ± 6.9	53.1 ± 8.0	35.3 ± 14.8

Abbreviations: 2D = 2-dimensional; CF = conventional fractionated; 3D = 3-dimensional; HOF = hypofractionated.

Table 2

Volumes in ccm and percentage of total volume that received a biologically equivalent dose of 54 Gy in midline structures, with 2D-CF (with daily 2.0 Gy) and 3D-HOF (with daily 2.5 Gy) regimens by anatomical location of tumour

	Lower brain stem		Upper brain stem	
Location of tumour	2D-CF	3D-HOF	2D-CF	3D-HOF
1. Frontobasal	0.0 0%	0.0 0%	4.3 16%	1.6 6%
2. Frontoparietal	0.0 0%	0.0 0%	1.1 3%	0.0 0%
3. Parietal-parafalcial	0.0 0%	0.0 0%	0.0 0%	0.6 2%
4. Parieto-occipital	0.0 0%	0.0 0%	0.0 0%	1.0 3%
5. Occipital	0.0 0%	0.0 0%	0.0 0%	0.0 0%
Average of 1–5.	0.0 ± 0.0	0.0 ± 0.0	1.1 ± 1.9	0.6 ± 0.7
6. Temporo-parieto-occipital	22.1 66%	2.06%	27.4 100%	11.0 40%
7. Temporal	19.7 57%	0.0 0%	30.5 87%	9.8 28%
8. Deep temporal	8.0 20%	0.1 0%	28.4 100%	17.0 60%
9. Temporo-parietal	3.8 10%	0.0 0%	30.2 100%	7.3 24%
10. Frontotemporo-parietal	8.2 20%	0.0 0%	30.2 100%	3.3 11%
Average of 6–10	12.4 ± 8.0	0.4 ± 0.9	29.3 ± 1.4	9.7 ± 5.1
Average of 1–10	6.2 ± 8.4	0.2 ± 0.6	15.2 ± 15.0	5.2 ± 5.9

Abbreviations: 2D = 2-dimensional; CF = conventional fractionated; 3D = 3-dimensional; HOF = hypofractionated. (Total volumes of the lower and upper brain stem in ccm for patients 1–10: 37.3 and 26.8; 36.5 and 37.7; 35.1 and 28.5; 34.5 and 31.9; 38.3 and 26.0; 33.5 and 27.4; 34.6 and 35.0; 40.1 and 28.4; 38.0 and 30.2; 40.8 and 30.2, respectively.)

10.7 ± 12.7 ccm for 2D-CF ($p = 0.0006$), resulting in a 16 ccm volume sparing on average per patient. However, for patients 3 and 4 the V-BED54 values of the UBS are higher by less than 1 ccm in the 3D-HOF treatment. Considering both the IBED and V-BED54 values, the advantages of the conformal treatment planning are more pronounced for tumours with temporal locations.

For visual evaluation of the biological dose distributions, CT slices at the level of the upper part of the eyes were chosen (Figs. 2 and 3). The visualization of isoeffect distribution also proved that with 3D-HOF the dose to midline structures was generally less than that with the 2D-CF treatment plans. The biological dose to midline structures with 3D-HOF did not exceed the 80% isodose values, but with traditional 2D-CF treatment planning it did (patient 10, Fig. 2). However, in the case of an insular tumour, the spatial overdosing of the UBS can be too high, mainly when we examined the regimen with no concomitant boost. The biological dose values over 100% to the midline areas cannot be avoided with HOF (patient 8, Fig. 3).

The cumulative DVHs of the two fractionation schemes for patients 10 and 8 are shown in Fig. 4 and 6. In Fig. 4 the advantages of the 3D-HOF regimen are demonstrated. The DVH curves are less steep with 3D-HOF than with 2D-CF with regard to both the LBS and UBS (see Fig. 4 caption), indicating a decreased probability of complications of the brain stem. Conversely, in the case of the insular tumour (patient 8) the analysis of DVH shows that with 3D-HOF treatment without concomitant boost, a significant part of the UBS received more than 100% of the biological dose (Fig. 5).

DISCUSSION

Malignant gliomas are characterized by local aggressiveness and moderate or low radiosensitivity (1–4). For CF external beam RT at a total dose of 60 Gy the tumor progression-free interval is short, mainly in patients having glioblastoma histology and/or other poor prognostic factors (1, 2). The introduction of image-based conformal methods actually encourages clinicians to be more accurate in dose placement and in acquisition of detailed dose distributions, with an option of dose escalation. Recent studies reported dose escalation up to 90 Gy with teletherapy or even higher total dose with brachytherapy or stereotactic RT boost (3, 4, 9, 19). Such a dose escalation can improve local control for selected patients. In addition, the treatment time is longer and the risk of radionecrosis is high, with the possible consequence of salvage neurosurgery (3, 19). Recently, accelerated-hyperfractionated RT regimens have been used to maximize the therapeutic ratio and shorten the overall treatment time. However, hyperfractionated regimens have no or minimal effect on survival in malignant gliomas (24–26). Nevertheless, two or three fractions have to be given per day in order to impede sublethal damage repair processes as well (11).

We studied an alternative way of dose escalation using an HOF RT regimen without total dose reduction (TDR). Malignant gliomas are radioresistant tumours with rapid proliferation properties and may have lower α/β ratios, factors that can predict higher response rates to HOF (8, 10, 11, 24, 27, 28). However, HOF as per definition means the reduction of total dose, and for external beam RT in practice generally, HOF regimens are the simplest treat-

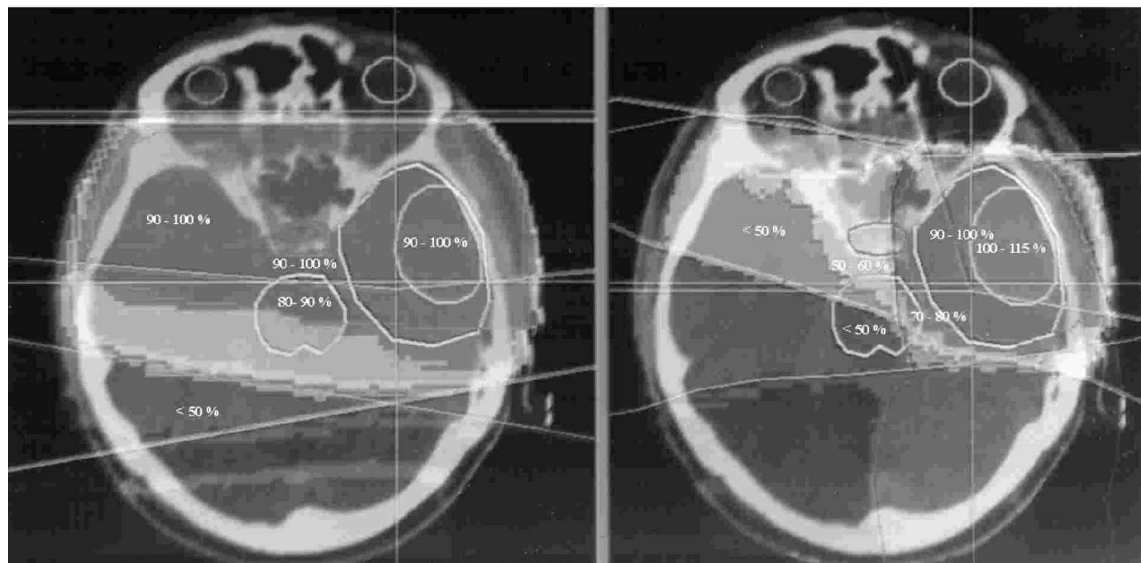


Fig. 2. The 2D-CF (left) and the 3D-HOF (right) treatment plans at the level of the upper part of the eyes (patient 10). In the 2D version coplanar weighted opposed 2-2 fields, in the 3D version 3-3 non-coplanar conformal fields with 6 and 18 MV-x energies were used. Note that biologically transformed dose values at the midline areas are lower with the conformal method, despite hypofractionation (50–70% vs. 80–100%).

ment methods in minimizing patient distress and optimizing cost effectiveness. The CNS tissues are fairly sensitive to large single doses, therefore to date, HOF is recommended only for patients with a poor prognosis (8, 24, 29). In previous studies using 2D techniques and HOF RT regimens, total dose was reduced to avoid neurotoxicity (3, 24, 29). One of the most aggressive therapeutic approaches used by Kleinberg et al. (29) suggests a total dose of 17×3 Gy for patients with advanced disease. Using focal RT,

Hulshof et al. (8) studied 4×7 Gy and 8×5 Gy HOF regimens for patients with a poor prognosis. They also suggested further investigation of 3D-HOF schedules for patients with a more favourable prognosis.

To our knowledge, no other studies have analysed the isoeffect distribution in different anatomical structures using external beam RT with different fractionation schemes and with the same total dose. In our model study we conducted exploratory analyses to determine whether 3D

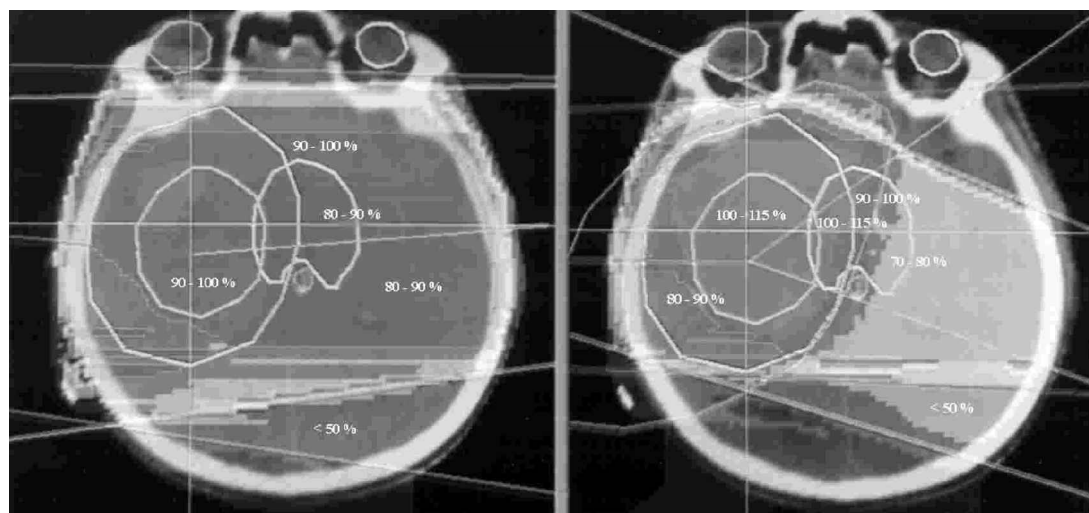


Fig. 3. Biological dose distributions with 2D-CF (left) and 3D-HOF (right) in a deep temporal tumour location (patient 8). In the 2D version coplanar weighted opposed 2-2 fields, in the 3D version 3-3 non-coplanar conformal fields with 6 and 18 MV-x energies were used. Biologically transformed doses were over 100% in the UBS with the 3D-HOF treatment plan, compared with dose values of 80–100% with the 2D-CF treatment plan.

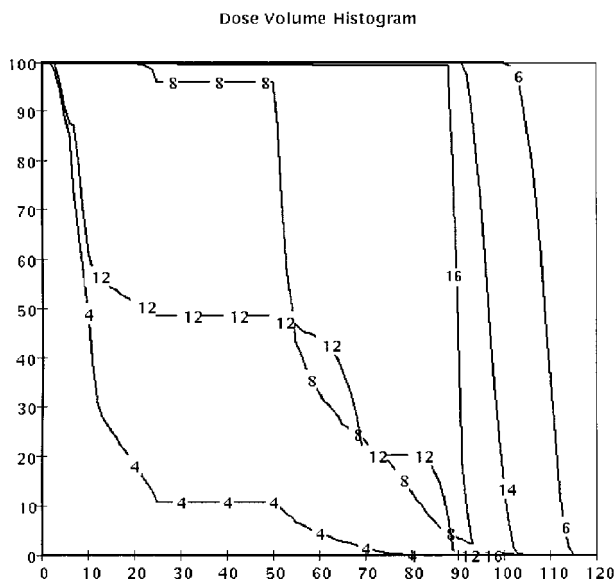


Fig. 4. The analysis of the cumulative biological dose-volume histograms of 3D-HOF and 2D-CF regimens with regard to the lower brain stem (LBS), upper brain stem (UBS) and the boost target (patient 10). With 3D-HOF, despite hypofractionation, the dose values to LBS and UBS are much lower (4 and 8) than those with 2D-CF (12 and 16). Note that the average relative biological dose of the boosted target with 3D-HOF was higher than that with 2D-CF (6 vs. 14), with a maximum value of about 115%. Conceptually, this means a higher probability of neurotoxicity, and a simultaneously higher biologically effective tumour dose.

conformal RT would ensure the possibility for biological dose escalation without increasing normal tissue toxicity. Our results confirmed the advantages of 3D-HOF treatment over the traditional 2D-CF irradiation with regard to the midline dose, even when HOF without TDR is used. The magnitude of a volume-sparing effect with 3D-HOF depends on the location and size of the target volume. Nevertheless, the target volume includes considerable normal brain tissues as well, with potential involvement of malignant cells. We endeavoured to avoid the normal tissue toxicity within the target volume using the shrinking field method and this resulted in a fall in biologically modified dose values in the transitional zone. Moreover, we developed a model that is suitable for analysing the effect of different treatment techniques and fractionation schedules on the spatial biological dose distribution and this model could be the basis for future developments. We can also examine the dose inhomogeneity that has a great significance in the biological effect of HOF (20).

From other studies dealing with brain-stem toxicity, Clark et al. (23) found the IBED values to be comparable with the probability of LBS complication after stereotactic RT, applying different fractionation schemes. They assigned the 60 Gy IBED as the tolerance limit of the LBS using an α/β value of 2.5 Gy. We used a lower α/β value (2.0 Gy) to emphasize the effect of HOF, but we did not

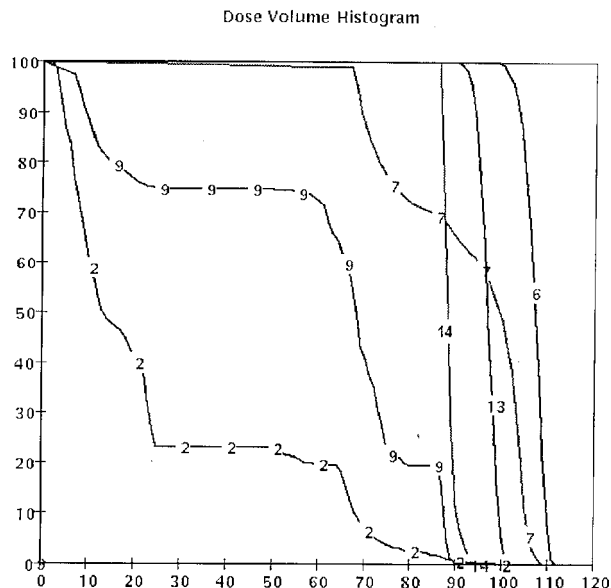


Fig. 5. Comparison of the cumulative biological dose-volume histograms of 3D-HOF to 2D-CF regimens with regard to the lower brain stem (LBS) (2 and 9), upper brain stem (UBS) (7 and 14) and the boost target (6 and 13) in patient 8 without a concomitant boost radiotherapy (RT) regimen. With 3D-HF, the dose values to UBS are unacceptably high—over 100% biologically transformed doses.

observe IBED values over 60 Gy with 3D-HOF in either UBS or LBS. The IBED values ranged from 1.7 Gy to 50.2 Gy. In contrast, with traditional 2D-CF, the IBED values of the UBS ranged from 58.5 Gy to 60.4 Gy in temporal tumour locations.

Debus et al. (18) described how in conformal, mixed photon and proton RT of skull base tumours, the LBS toxicity is affected by the volume of 'high-dose regions' (mainly over 60 CGE—cobalt equivalent gray units) rather than by the maximum dose value. They found 2.7 ccm for the threshold volume of LBS toxicity over a 55 CGE dose. We selected 54 Gy as the limiting dose value for our analysis. We calculated 2.0 ccm as the highest value of V-BED₅₄ in the LBS, but in 8 out of 10 cases (80%) there was no high-dose volume with 3D-HOF. On the contrary, in the UBS, the V-BED₅₄ values were up to 17 ccm with 3D-HOF. Nevertheless, in 7 out of 10 cases (70%) the values with 3D-HOF were lower than those with 2D-CF. In the study by Clark et al. (23), late toxicity occurred when the volume irradiated over a 60 Gy biologically effective dose surpassed 18% of LBS. Assigning 54 Gy as the biological limiting dose and applying 3D-HOF, the percentage of 'high-dose regions' was over 18% only in UBS (range 0% to 60%). In contrast, with 2D-CF, the percentage of 'high-dose regions' in LBS was between 0% and 66%, and in UBS, considering temporal locations, these values were about 100%.

In conclusion, the results of our model study show that 3D HOF RT without TDR may be the therapeutic choice in the treatment of suprasellar lobar glioblastomas. However, the anatomical location and the volume of the target can influence the validity and feasibility of HOF. The advantage of these regimens is a shorter RT treatment course with higher biological target dose. Prospective clinical studies are required to choose the optimal fractionation schedules and to justify that this 3D HOF approach does indeed improve local control rate without increasing normal tissue toxicity.

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